The influence of suspended particles on the mass transfer at a rotating disc electrode. Non-conducting particles

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The influence of suspended SiC particles on the mass transfer at an RDE (rotating-disc electrode) was investigated for the reduction of K_3 Fe(CN)₆ and ZnO in alkaline electrolyte. A model for the increased mass transfer is developed, based on the decrease of the diffusion layer thickness by rotation of the particles in this layer. In experiments with different volume fractions of suspensions a critical value in the rotation speed and in volume fraction is found. The influences of hydrodynamic conditions, gravity, particle size and adhesion between particles and electrode were studied to investigate the origin of both critical values.

Nomenclature

- A area (m²) A_{132} Hamaker constant with liquid 3 between
- *a* materials 1 and 2 (Nm) *a* particle radius (m)
- B function defined in Equation 20 (A s^{1/2} rad^{-1/2})
- c concentration of the reactants (mol m⁻³)
- D diffusion coefficient (m² s⁻¹)
- *d* local decrease of the diffusion layer thickness at a particle position (m)
- \overline{d} average decrease of the diffusion layer thickness at a particle position (m)
- *e* shear rate component (s^{-1})
- F force on a particle (N)
- g gravitational constant (m s⁻²)
- *h* distance between two particles (m)
- H dimensionless velocity in the z-direction
- I current (A)
- k time constant (s⁻¹)
- *K* correction factor on the Stokes force for concentrated suspensions
- M total mass of all particles (g)
- $M_{\rm p}$ mass of one particle (g)
- *n* number of electrons
- N number of particles
- P pressure (Pa)
- r_0 radius of domain with active film transport (m)
- $r_{\rm E}$ electrode radius (m)
- r_1 radius from the centre of a particle in the x_1 , - x_2 plane (m)
- t time (s)
- *u* velocity disturbance (m s⁻¹)
- v velocity (m s⁻¹)
- x coordinate
- z (axial) coordinate, distance in z-direction (m)
- z_0 minimal approach distance between particles and RDE (m)
- ÿ shear rate (at a RDE) (s^{-1}) $\Delta \delta$ decrease of the diffusion layer thickness (m) $\delta_{\rm N}$ diffusion layer thickness (m) viscous boundary layer thickness (m) $\delta_{\rm P}$ dynamic viscosity (Pas) ŋ V angle between x_1 axis and r (rad) kinematic viscosity $(m^2 s^{-1})$ ν ξ dimensionless distance in z-direction to a RDE density $(kg m^{-3})$ ρ density difference between particle and liquid $\Delta \rho$ $(kg m^{-3})$ angular velocity of a particle (rad s^{-1}) ω ω_0 angular velocity is shear flow (rad s^{-1}) angular acceleration of a particle (rad s^{-2}) ŵ angular velocity of a RDE (rad s^{-1}) Ω volume fraction (vol %) φ bed expansion (vol %) 3 Superscript bulk solution S σ surface Subscript а adhesion с critical value, centre E electrode gravitation g i dimension index dimension index j k dimension index 1 diffusion limited Ν Nernst 0 outer particle р Ρ Prandtl R radial

radial direction

Stokes

r

S

1. Introduction

The rate of mass transfer of an electrode process can be enhanced via increased convection of the electrolyte, or by introducing turbulence promoters [1], gas bubbles [2, 3], and solid particles [4-20]. The influence of glass spheres was measured by Leitel et al. [4] and Roha [5] for a RDE (rotating disc electrode) and by Smith et al. [6] for an electrode in a tube wall. Roha [5] also studied the influence of the particle size and found a weak maximum in the mass transfer when the particle diameter equals the diffusion layer thickness. Studies with sand particles in tubes were carried out by Postlethwaith et al. [7, 8] and Heitz [9]. Zeilmaker et al. [10] studied the influence of CaCO₃ particles with an RDE electrode; Pini et al. [11] the addition of SiC at a rotating-cylinder electrode. Keller [12], Antonini et al. [13, 14] and Hyman [15] investigated a suspension of red blood cells in laminar flow cells (tubes). Caprani and co-workers [16-18] investigated the influence of suspensions of SiC, Al₂O₃, B₄C and red blood cells with a rotating-disc electrode, and gave a theoretical model [19]. Al₂O₃ suspensions were studied in a Couette cell by Deslouis et al. [20]. All investigations show a remarkable increase in mass transfer, in some cases up to 300%. It can easily be shown that the addition of particles cannot promote turbulence: the Reynolds number at an RDE with radius $(r_{\rm F})$ is

$$Re_{\rm F} = 2\Omega r_{\rm F}^2 / v \tag{1}$$

with Ω = angular velocity of the electrode; $\Omega = 2\pi f$; ν = kinematic viscosity. For R = 5 mm and rotation frequency f = 64 rps it follows that $\text{Re}_{\text{E}} = 25400$. For $\text{Re}_{\text{E}} < 10^5$ the flow at the RDE is laminar [21]. Addition of particles with diameter 1 to 50 μ m increases the viscosity of the electrolyte and hence decreases Re_{E} , so that turbulence will not occur.

The hydrodynamic flow around a particle with radius a is characterized by another Reynolds number

$$\mathrm{Re}_{\mathrm{p}} = 2\omega a^2 / v \tag{2}$$

with ω = angular velocity of the particle. This Reynold number is lower than 1 for a particle radius smaller than 4 μ m. So, Stokes flow conditions prevail around the particles. Also, surface renewal [5] due to the scraping of the particles or penetration into the diffusion layer cannot explain the large increase of mass transfer.

The most acceptable model is based on the rotation of the particles in the diffusion layer [12–20], which is caused by the rotation component of the shear field in the viscous boundary layer. This effect can be expressed [12–14] in terms of an effective diffusion coefficient which is determined by the shear rate ($\dot{\gamma}$) and the volume fraction, ϕ , of the particles.

The model of Hyman [15] is often used to calculate the limiting diffusion current [16–20]. For the rotating disc electrode this model predicts a linear $I_1-\Omega^n$ relation at high rotation speeds with n = 7/6 [16, 17, 19]. Caprani *et al.* [17] found experimentally that n = 0.5 for both low and high rotation rates, while at the intermediate rates n = about 0.6 was found. We also observed n = 0.5 with SiC suspensions [22]. It is difficult to see how blockage of the electrode can explain this discrepancy.

Several investigations [5, 18, 22] showed a threshold or critical value for the volume fraction, ϕ_c , and also for the rotation speed, Ω_c , above which particles affect the mass transfer. In this paper the effect of SiC particles on the mass transfer was studied with the rotating-disc electrode for the reduction of K₃Fe(CN)₆ and ZnO in alkaline solutions.

Hydrodynamic conditions, gravity direction to the electrode and particle size, were varied in order to investigate the effect on the critical values ϕ_c and Ω_c . A new model is developed, in which rotation of the particles causes a decrease of the average diffusion-layer thickness, while the value of the diffusion coefficient is expected to be unaffected by the particles. For the rotating-disc this model predicts a $I_1 - \Omega^{1/2}$ relation as given in the Levich equation, and an extra increase of the limiting current proportional to ϕ . The occurrence of a critical value of Ω and ϕ is also explained.

2. Experimental details

An electrochemical cell with a volume of 100 ml was used for the experiments. The electrolyte was 2M KOH with 0.05 M ZnO or with 0.05 M K₃Fe(CN)₆. The reference electrode for reduction of ZnO was an Hg/HgO electrode; for the reduction of K₃Fe(CN)₆ a saturated calomel electrode was used; both were provided with a Luggin capillary. A platinum electrode of area 6 cm² was used as the counter-electrode. Two platinum rotating-disc electrodes with radii $r_{\rm E} = 3$ and 5 mm were used, the electrodes were polished with Al₂O₃ paste down to 0.05 μ m. For the reduction of K₃Fe(CN)₆, a pyrolytic-graphite electrode with a radius of 4 mm was also used.

The average size of the SiC particles (arbitrary shape) for these experiments was determined from SEM photographs and is presented in Table 1. Before measurement a small quantity of powder was added to the electrolyte and stirred for about 5 min with a magnetic stirrer at the bottom of the cell. During the measurement, the magnetic stirring was stopped. The suspension was stirred between two measurements to avoid precipitation.

Table 1. Average size of the measured particle

Carborundum (SiC)		
Number	Average particle diameter, 2a (μm)	
1200	3.0	
800	6.6	
500	12.2	
280	36.4	
150	85.0	



Fig. 1. Voltammograms of the reduction of $0.05 \text{ M K}_3\text{Fe}(\text{CN})_6$ in 2M KOH at a pyrolytic graphite RDE; rotation frequencies of 16, 36 and 64 rps. (----) without particles (---) with 6 vol% SiC particles of 6.6 μ m diameter.

Coagulation of the particles during the experiments was not observed.

3. Results and discussion

Fig. 1 shows the voltammogram for the reduction of $0.05 \text{ M} \text{ K}_3 \text{Fe}(\text{CN})_6$ in 2 M KOH at the pyrolytic graphite electrode, the solid lines are measurements without particles; the dashed lines with 6 vol% SiC particles with a diameter of $6.6 \,\mu\text{m}$. The effect of



Fig. 2. Voltammograms of the reduction of 0.05 M ZnO in 2 M KOH at a platinum RDE ($r_{\rm E} = 4$ mm); rotation frequencies of 25 and 81 rps. (----) without particles (---) with 6 vol% SiC particles of 6.6 μ m diameter.



Fig. 3. Levich plot of the reduction of 0.05 M K₃Fe(CN)₆ in 2 M KOH at a platinum RDE ($r_E = 3 \text{ mm}$) with the following volume fractions (vol%) of SiC particles of 6.6 μ m diameter: (+) 0 (Δ) 6 (\odot) 10 (**m**) 15 (Δ) 20 (**o**) 25.

6 vol% SiC on the reduction of ZnO at a platinum electrode is presented in Fig. 2. Both figures show an increased mass transfer after addition of the SiC particles. In Fig. 3 the Levich plot $(I_1 - \Omega^{1/2})$ is given for the reduction of K_3 Fe(CN)₆ for different volume fractions of the particles; the influence of the volume fraction on the limiting current is seen in Fig. 4. In Figs 5 and 6 the limiting current is plotted as a function of the square root of the rotation speed and the volume fraction. In this experiment the disc radius, r_E , is 5 mm and the SiC particle diameter is 12.2 μ m. In Figs 3 and 5 the Levich equation is obeyed from zero to low SiC content; at higher volume fractions, a



Fig. 4. Limiting current (taken from the data of Fig. 3) as a function of the volume fraction (ϕ) at rotation frequencies in rps of (+) 4 (Δ) 9 (\bigcirc) 16 (\blacksquare) 25 (\blacktriangle) 36 (\bigcirc) 49 (∇) 64 (\diamondsuit) 81.



Fig. 5. Levich plot of the reduction of 0.05 M K₃Fe(CN)₆ in 2 M KOH at a Pt-RDE ($r_E = 5 \text{ mm}$) with the following fractions (vol%) of SiC particles of 12.2 μ m diameter: (+) 0 (\triangle) 5 (\bigcirc) 10 (\blacksquare) 15 (\triangle) 20.

critical rotation frequency, Ω_c , is observed, above which the enhanced mass-transfer is seen. Above Ω_c the slope increases with an increasing volume fraction of the particles. In Figs 4 and 6 also a critical value for the volume fraction, ϕ_c , is also observed. It thus appears that only above Ω_c and ϕ_c do particles increase the mass transfer.

The effect of particle size was investigated for SiC particles with diameters 6.6, 12.2 and 36.4 μ m. In Figs 7–9 the limiting current for the reduction of K₃Fe(CN)₆ is depicted as a function of $\Omega^{1/2}$ and in Figs 10–12 as a function of the volume fraction.



Fig. 6. Limiting current (taken from the data of Fig. 5) as a function of the volume fraction (ϕ) at rotation frequencies in rps of (+) 4 (Δ) 9 (\odot) 16 (**■**) 25 (\blacktriangle) 36 (**●**) 49 (∇) 64.



Fig. 7. Levich plot of the reduction of K_3 Fe(CN)₆ at a pyrolytic graphite RDE ($r_E = 4 \text{ mm}$) with the following fractions (vol%) of SiC particles of 6.6 μ m diameter: (+) 0 (Δ) 3 (**■**) 6 (\blacktriangle) 11 (**●**) 16 (\bigtriangledown) 20.

4. The model

In Fig. 13a the hydrodynamic conditions adjacent to an electrode are depicted. In this layer with thickness $\delta_{\rm P}$ a shear rate $\dot{\gamma} = dv/dz$ exists, which can be seen as the sum of a pure streaming motion ($v_{\rm s}$) and a rotational flow field with angular rotation frequency $\omega_0 = \frac{1}{2}\dot{\gamma}$. If microscopic particles are present in the electrolyte flow along an electrode surface, this rotational flow field also induces a particle rotation, $\omega_0 = \frac{1}{2}\dot{\gamma}$, due to the viscous forces (Fig. 13b). The torque (T) acting on a spherical particle with radius a is, according to



Fig. 8. Levich plot of the reduction of K_3 Fe(CN)₆ at a pyrolytic graphite RDE ($r_E = 4 \text{ mm}$) with the following fractions (vol%) of SiC particles of 12.2 μ m diameter: (+) 0 (Δ) 4 (O) 6 (**I**) 11 (Δ) 16 (**O**) 20 (∇) 24.



Fig. 9. Levich plot of the reduction of K_3 Fe(CN)₆ at a pyrolytic graphite RDE ($r_E = 4 \text{ mm}$) with the following fractions (vol%) of SiC particles of 36.4 μ m diameter: (+) 0 (\triangle) 6 (\bigcirc) 10 (\blacksquare) 16 (\blacktriangle) 20 (\bigcirc) 25 (\bigtriangledown) 29.

Brenner [23]

$$T = 64 \pi \eta a^3(\omega_0 - \omega). \tag{3}$$

with η = dynamic viscosity. This torque gives the particle, with moment of inertia J an angular acceleration $\dot{\omega}$

$$T = \dot{\omega}J \tag{4}$$

The moment of inertia of a spherical particle is

$$J = (8/15) \pi a^{5} \rho$$
 (5)

with ρ = density of particle. So it follows from Equations 3-5 that



Fig. 10. Limiting current as a function of the volume fraction (ϕ) of 6.6 μ m SiC particles at rotation frequencies in rps of (+) 16 (Δ) 25 (\odot) 36 (\blacksquare) 49 (\blacktriangle) 64.



Fig. 11. Limiting current as a function of the volume fraction (ϕ) of 12.2 μ m SiC particles at rotation frequencies in rps of (+) 16 (Δ) 36 (O) 64.

with $k = 120 \eta / \rho a^2$. The solution of this differential equation is:

$$\boldsymbol{\omega} = \boldsymbol{\omega}_0 \left(1 - \mathrm{e}^{-kt} \right) \tag{7}$$

For particles with a radius smaller than $20 \,\mu\text{m}$, $\rho = 3000 \,\text{kg m}^{-3}$ and $\eta = 1.2 \times 10^{-3} \,\text{kg s}^{-1} \,\text{m}^{-1}$, the time constant, k, is larger than $10^5 \,\text{s}^{-1}$. This implies that at the rotation frequency $\omega_0 = \frac{1}{2}\dot{\gamma}$, the particles rotate within about 10 μ s after entry. Due to this short response time the particles rotate at a frequency of about ω_0 and notwithstanding the short time, (~ 200 ms) the particles actually pass along the RDE surface.



Fig. 12. Limiting current as a function of the volume fraction (ϕ) of 36.4 μ m SiC particles at rotation frequencies in rps of (+) 4 (Δ) 16 (\bigcirc) 36 (\blacksquare) 64.











The velocity disturbance (u) of the rotating particles, besides the normal shear field, v, can be calculated using an expression given by Batchelor [24]. This flow field is superposed on the normal existing field, v, in the viscous boundary layer. For one velocity direction, u_i

$$u_i = -e_{ij}x_j\left(\frac{a}{r}\right)^5 + \frac{5}{2}e_{jk}x_ix_jx_k\left[\left(\frac{a}{r}\right)^7 - \left(\frac{a}{r}\right)\right]^5$$
(8)

with

$$e_{ij} = \frac{1}{2} \left(\frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right)$$
(9)

e is the shear rate and x_i is the distance in one direction from the centre of the particle.

Fig. 13. (a) Hydrodynamic boundary layer δ_p at an electrode. (b) Rotating speed (ω) in the x_2 -direction of a particle with a velocity disturbance (u) in the x_1 - x_2 plane and $x_3 = z = 0$. (c) Velocity field around a rotating particle with radius *a* (coordinates moving along with the particle translation velocity). Domains of closed and open streamlines are seen, separated with the broken line. (d) Sphere with radius r_0 of increased mass transfer. The decrease of the diffusion layer is *d* for the ring with a surface $2\pi r dr$. (e) Concentration profile of the active ions at an electrode. Without a particle the diffusion layer thickness is δ_N ; with a rotating particle, the layer thickness becomes $\delta_N - \Delta \delta$.

The velocity disturbance component, u_3 , in the z direction contributes to an extra mass transfer to the electrode (see Fig. 13b). Considering simple shear conditions in one direction $v_1 = \dot{\gamma}x_3$, $v_2 = 0$ and $v_3 = 0$ this gives only two shear rate components

$$e_{13} = e_{31} = \frac{1}{2} \left(\frac{\partial v_1}{\partial x_3} + \frac{\partial v_3}{\partial x_1} \right) = \frac{1}{2} \dot{y}$$
 (10)

At the point P in Fig. 13b, $x_1 = r \cos \psi$, $x_2 = r \sin \psi$ and $x_3 = 0$ and the disturbance velocity becomes

$$u_{3} = e_{3j}x_{j}\left(\frac{a}{r}\right)^{5} = -e_{31}x_{1}\left(\frac{a}{r}\right)^{5}$$
$$= -\frac{1}{2}\dot{\gamma}r\left(\frac{a}{r}\right)^{5}\cos\psi \qquad (11)$$

For the total disturbance velocity, *u*, we can also write:

$$\boldsymbol{u} = -(\boldsymbol{\omega}_0 \times \boldsymbol{r}) \left(\frac{a}{r}\right)^5 \cos \psi \qquad (12)$$

The disturbance, u, evoked by strain forces on the particle, gives a different flow pattern around a particle in the viscous boundary layer [25] as shown in Fig. 13c. Domains of closed and open streamlines are seen, separated at the broken line in this figure. In the domain of closed streamlines the reactants are well mixed.

Due to the rapid decrease of the velocity disturbance |u| with the distance to the particle, the domain will be small compared with the particle size, therefore film transport of the reactant at the particle surface can be assumed (see Figs. 13c). Due to the reaction of the active species, a concentration gradient exists in the zdirection to the electrode surface. For the particles in this diffusion layer an average concentration is assumed in the domains of closed streamlines (Fig. 13c). This results in a local decrease of the diffusion layer thickness, d, which depends on the distance, r, from the zaxis of the particle in Fig. 13d. In this figure r_0 is the distance to the centre of the particle where |u| is equal to the rate of mass transfer of the reactants without particles. For a radius greater than r_0 no increase of mass transfer exists. The average thinning, \overline{d} , of the diffusion layer for a film thickness $|r_0 - a|$ around the particle is

$$\bar{d} = \frac{\int_{0}^{r_{0}} d(r) 2\pi r dr}{\int_{0}^{r_{0}} 2\pi dr} = \frac{4\pi \int_{0}^{r_{0}} (r_{0}^{2} - r^{2})^{\frac{1}{2}} r dr}{2\pi \int_{0}^{r_{0}} r dr} = \frac{4}{3} r_{0}$$
(13)

This holds for the cross-sectional area of the particle $A_{\rm p} = \pi r_0^2$.

For an electrode surface $A_{\rm E} = \pi r_{\rm E}^2$, the average thinning for N particles in the diffusion layer is

$$\Delta \delta = \frac{4}{3} r_0 \frac{A_p}{A_E} = \frac{4r_0^3 N}{3r_E^2}$$
(14)

Fig. 13e presents the concentration profile at an electrode, with and without particles. It is assumed that one particular particle does not disturb the velocity distribution around other particles, and that the particle size is smaller than the diffusion layer thickness ($2a < \delta_N$). The volume fraction of the particles can be expressed by $\phi = V_d/(V_0 + V_d)$, where V_d is the total particle volume and V_0 is the volume of the liquid. The number of particles, N, is defined as

$$N = \frac{M}{M_{\rm p}} = \frac{\phi V_0}{\frac{4}{3} \pi a^3 (1 - \phi)}$$
(15)

with M = total mass of all particles in the diffusion layer and $M_p =$ the mass of one particle.

Only particles present in the diffusion layer increase the mass transfer; the volume of this layer is $V_0 = \pi r_{\rm E}^2 \delta_{\rm N} (1 - \phi)$, therefore

$$N = \frac{\pi \phi r_{\rm E}^2 \delta_{\rm N}}{\frac{4}{3} \pi a^3} \tag{16}$$

Substitution in Equation 14 leads to

$$\frac{\Delta\delta}{\delta_{\rm N}} = \left(\frac{r_0}{a}\right)^3 \phi \tag{17}$$

The relative decrease of the diffusion-layer thickness is thus proportional to the volume fraction of the particles in this layer and the ratio r_0/a .

The limiting current is given by

1

$$I_{\rm i} = nFA_{\rm E}Dc^{\rm s}/\delta_{\rm N} \tag{18}$$

For an RDE

$$Y_1 = B\Omega^{1/2} \tag{19}$$

with

$$B = 0.62 \, nFA_{\rm E} D^{2/3} v^{-1/6} c^{\rm s} \tag{20}$$

Reduction of the diffusion layer by the spinning particles is $\delta_N - \Delta \delta$, so with Equations 18 and 19

$$I_1 = B\Omega^{1/2}/(1 - \Delta\delta/\delta_N)$$
(21)

Substitution from Equation 17 gives

$$I_1 = B\Omega^{1/2} / \left[1 - \left(\frac{r_0}{a}\right)^3 \phi \right]$$
(22)

This expression is only valid for a low fraction of particles. Then no overlap of the space domain of the rotating particles is considered. Expansion in a Taylor series and neglecting higher terms yields

$$I_1 = B\Omega^{1/2} \left[1 + \left(\frac{r_0}{a}\right)^3 \phi \right]$$
(23)

The limiting current can thus be expressed as a modified Levich equation which takes into account the volume fraction, ϕ , of the particles and the ratio r_0/a .

Figs 4 and 6 show a linear relationship between I_1 and ϕ in good agreement with Equation 23. Plots of the experimental results according to Equation 22, however, do not yield a straight line. It seems that the error introduced by going from Equation 22 to Equation 23 is compensated.

This could be due to the overlap of the space domains of the rotating particles, in particular at higher volume fractions.

This model does not predict the appearance of the critical values in Ω and ϕ as measured in Figs 3–12. Four explanations of the origin of the values Ω_c and ϕ_c will now be further investigated

1. Changes in hydrodynamic conditions.

2. Gravity forces which cause precipitation.

3. Critical peripheral rotation velocity of the rotating particle which is proportional to the particle size.

4. Adhesion of the particles to the electrode and blockage of the electrode.

4.1. Hydrodynamic conditions

The ratio of the inertial forces and viscous forces of the mass flow near the electrode may be crucial. This is characterized by the Reynolds number of the elec-

Parameter	Experiment 1	Experiment 2
Particle size, $2a \ (\mu m)$	6.6	12.2
Electrode radius, $r_{\rm E}$ (mm)	3.0	5.0
Outer electrode radius, r _o (mm)	6.2	13.0
Results		
Critical rotation speed, $\Omega_c^{1/2}$ [(rad s ⁻¹) ^{1/2}]	10.0	5.1
Critical volume fraction, ϕ_c (vol %)	2.5	3.8

Table 2. Parameters and results for two disc-electrode experiments

trode $\text{Re}_{\text{E}} = 2 \Omega r_{\text{E}}^2 / v$, and of the particle $\text{Re}_{\text{p}} = 2 \omega a^2 / v$. To establish this effect on Ω_{c} and ϕ_{c} , the limiting current was compared for two systems under similar hydrodynamic conditions, Figs 3 and 4 and Figs 5 and 6. In these experiments two disc electrodes were used with radii r_{E1} and r_{E2} and two different particle sizes. The particle sizes were chosen such that the ratios $\text{Re}_{\text{E}}/\text{Re}_{\text{p}}$ were the same for both systems. This requires $a_1/a_2 = r_{\text{E1}}/r_{\text{E2}}$ at the same rotation frequency.

Because the hydrodynamic conditions also depend on the outer radius r_0 of the electrode, $a_1/a_2 = r_{E1}/r_{E2} = r_{01}/r_{02}$. The parameters and results of both experiments are summarized in Table 2.

For the same ratio of inertial/viscous forces in the boundary layer, the critical frequency, Ω_c , and critical volume fraction, ϕ_c , for both experiments differ. This excludes the hydrodynamic effect as being responsible for the appearance of the values Ω_c and ϕ_c .

4.2. Gravitation

The influence of gravitation on the appearance of a



Fig. 14. Levich plot of the reduction of 0.05 M K₃Fe(CN)₆ in 2 M KOH in an upside-down cell at a pyrolytic graphite RDE ($r_E = 4 \text{ mm}$) with the following fractions (vol%) of SiC particles of 6.6 μ m diameter: (+) 0 (Δ) 5 (\odot) 10 (\blacksquare) 15 (Δ) 20.

critical volume fraction was investigated in an upsidedown cell: a 200 ml cell in which the RDE was mounted at the bottom. Six small (1 cm wide \times 5 cm high) baffles were inserted in the upper part of the cell to prevent a strong circulation of electrolyte and sucking of air to the electrode. A small stirrer in the upper part of the cell prevented precipitation of the suspension. For these experiments, a pyrolytic graphite RDE with a radius of 4 mm was used and SiC particle sizes of 6.6 and 12.2 μ m. The results for the limiting current as a function of the rotation speed and the volume fraction are shown in Figs 14–17. In Figs 15 and 17, a critical volume fraction, ϕ_c , is absent, however a critical rotation speed, Ω_c , is observed (Figs 14 and 16).

In Figs 15 and 17, the drawn lines are the best fit of Equation 23 with $r_o/a = 1.65$. As can be seen from both figures, the model gives a good agreement for the higher rotation speeds, $\Omega > \Omega_c$. For the experiment with a particle size of $12.2 \,\mu\text{m}$, the diffusion layer thickness $\delta_N = 7 \,\mu\text{m}$ for a rotation speed of 64 rps, which indicates that in this case, for a particle size larger than the diffusion layer thickness, the model



Fig. 15. Limiting current (taken from the data of Fig. 14) as a function of the volume fraction (ϕ) at rotation frequencies in rps of (+) 4 (Δ) 9 (O) 16 (**II**) 25 (\blacktriangle) 36 (\bullet) 49 (∇) 64. The drawn lines are fitted with Equation 23.



Fig. 16. Levich plot of the results with an upside-cell with particle diameter of $12.2 \,\mu$ m (other data and key as in Fig. 14).

does not fully agree with the experimental results (Fig. 17).

The gravitational force acting on a particle with radius a in suspension is

$$F_{\rm g} = \frac{4}{3} \pi a^3 \Delta \rho g \tag{24}$$

with $\Delta \rho$ = the difference between particle density and the liquid density. This force induces a precipitation of the particles. For dilute suspensions, the precipitation velocity is retarded by the Stokes force

$$F_{\rm S} = 6\pi \eta a \Delta v \tag{25}$$

 Δv = the difference between the particle velocity and the liquid velocity. At a distance to the electrode that is comparable with the viscous boundary-layer thick-



Fig. 17. Limiting current (taken from the data of Fig. 16) as a function of the volume fraction (ϕ) at the same rotation frequencies. See Fig. 15 for key. The drawn lines are fitted with Equation 23.

ness, $\delta_{\rm P}$, a small pressure gradient dp/dz causes an extra force $(F_{\rm p})$ on the particles

$$F_{\rm p} = \frac{4}{3} \pi a^3 \frac{\mathrm{d}p}{\mathrm{d}z} \tag{26}$$

The viscous and pressure forces are in equilibrium with the gravitational force

$$F_{\rm g} - F_{\rm S} + F_{\rm p} = 0 \tag{27}$$

This yields the precipitation velocity

$$\Delta v = \frac{2}{9} \frac{a^2}{\eta} \left(\Delta \rho g + \frac{\mathrm{d} p}{\mathrm{d} z} \right) \tag{28}$$

The mass transfer at an RDE depends strongly on the electrolyte flow to the electrode, i.e. the flow in the axial direction, v_z . This flow only depends on the z coordinates of the electrode and is $v_z = (\Omega v)^{1/2} H(\xi)$ [21] where $H(\xi)$ is a dimensionless velocity depending on the dimensionless distance to the electrode $\xi = (\Omega/v)^{1/2}$. For small distances $z \leq \delta_p$, the axial velocity is a parabolic function of the distance [21]

$$v_z = 0.51 \Omega^{3/2} v^{-1/2} z^2 \tag{29}$$

For an electrode facing down, the particles cannot always reach the electrode surface. Then in the centre of the RDE (r = 0), the particles are at the minimal approach distance to the RDE because the radial and angular velocities are zero.

At this smallest distance, z_0 , the upward velocity, v_z , is equal to the precipitation velocity, Δv . From Equations 28 and 29 it follows

$$z_0 = -0.66 \frac{a v^{1/4}}{\eta^{1/2} \Omega^{3/4}} \left(\Delta \rho g + \frac{\mathrm{d} p}{\mathrm{d} z} \right)^{1/2} \qquad (30)$$

The minimal approach distance, z_0 , is proportional to the radius, a, of the particle. For an SiC particle with radius $a = 2.5 \,\mu\text{m}$, $z_0 = 3.5 \,\mu\text{m}$ at a rotation speed $\Omega = 314 \,\text{rad s}^{-1}$. The distance between particle and electrode is comparable with the diffusion-layer thickness, δ_N , therefore these particles cannot influence the mass transfer to the electrode. This explains why no influence of the particles is observed at low volume fractions in Figs 4 and 6.

Roha [5] has numerically calculated the minimal distance between particles and the RDE for a suspension of glass spheres and called this the 'static approach distance'. Because of such a region without particles, there will be a region with an increased number of particles at larger distance and it can be argued that this 'condensed layer' has fluidised-bed properties. With increasing volume fractions of particles of this fluidised bed, the fall-velocity of the particles according to the Stokes equation will decrease with a factor $K(\phi)$.

This correction $K(\phi)$ depends on the volume fraction of the particles and is the result of the increased viscosity and hindrance by other particles. This correction can be derived from the relation given by Barnea and Mizraki [26]. Instead of the bed expansion, ε , K is given here as a function of the volume fraction, ϕ

$$K(\phi) = \frac{(1-\phi)^2}{(1+\phi^{1/3})\exp\left[5\phi/3(1-\phi)\right]} \quad (31)$$

By adding more particles, the volume fraction increases and the volume fraction of the particles in the condensed layer becomes higher than the bulk value. This effect together with $K(\phi)$ gives an extra increase of the volume fraction of particles in the condensed layer and results in a strongly reduced fall-velocity of the particles and hence a smaller z_0 .

If z_0 becomes smaller than δ_N , the particles also affect the diffusion boundary-layer and thus the mass transfer. So there will be a critical volume fraction above which an enhanced mass transfer is noticed (Figs 4 and 6). Equation 30 predicts that z_0 is proportional to $\Omega^{-3/4}$. Experimentally only a slightly higher ϕ_c is observerd in Fig. 4 for the lower rotation frequencies.

In principle the gravitation effect is similar to the collision induced model of Roha [5], however instead of considering the increased viscosity by adding more particles, he calculated the increase in number of collisions of the particles above which the particles penetrate the diffusion layer and so increase the mass transfer.

Caprani *et al.* [16, 17] did not observe a critical volume-fraction in experiments with an electrolyte with higher viscosity. With addition of 60% glycerol, the viscosity, η , increases and reduces the distance, z_0 (compare with Equation 30) without particles. This reduction was so large that no critical volume fraction was observed.

4.3. Particle size

It can be expected that the critical volume fraction depends on the particle size. It was shown (Equation 30) that linear relation exists between the layer thickness, z_0 , without particles and the particle size. Because a larger particle size also yields a thicker layer, z_0 , a higher critical volume fraction, ϕ_c , is to be expected. Figs 10–12 show that ϕ_c indeed increases with particle size and that I_1 increases nearly linearly with ϕ , with the highest increase for the largest particles. Fig. 18 presents the correlation between ϕ_c and particle size for both processes of K_3 Fe(CN)₆ and ZnO reduction. For the reduction of K_3 Fe(CN)₆, a proportional relation between critical volume fraction, ϕ_c , and the particle size *a* is found.

However, a deviation of this proportionality is observed for the reduction of ZnO, especially for the smaller particles. A possible explanation could be the formation of zinc particles that coagulate with the SiC particles. The influence of the particle size on the critical rotation speed is shown in Figs 7–9. The critical rotation speed, Ω_c , observed in these figures, is given as a function of the particles size in Fig. 19. The critical rotation speed, Ω_c , is the same for both reduction processes and is proportional to the reciprocal particle size or $\Omega_c \sim 1/a$.



Fig. 18. The critical volume fraction (ϕ_c) as a function of the particle size (2*a*) for the reduction of (\triangle) K₃Fe(CN)₆ and (+) ZnO.

The appearance of a critical value of the rotation speed, above which the influence of particles on mass transfer is noticeable, indicates that a certain value of the peripheral velocity (v_p) of the rotating particle is required which contributes to extra mass transfer, due to a normal electrolyte velocity component to the RDE. The rate of mass transfer (v_z) is the result of convection and diffusion to the electrode. The particle peripheral rotation velocity (v_p) is: $v_p = \omega_0 a$.

This rotation speed depends on the shear rate ($\dot{\gamma}$) at a RDE [16–18] which is given by

$$\dot{\gamma} = 0.8 \,\Omega^{3/2} v^{-1/2} r_{\rm E} \tag{32}$$

This gives, with $\omega_0 = \frac{1}{2}\dot{\gamma}$,

$$v_{\rm p} = 0.4 \,\Omega^{3/2} v^{-1/2} r_{\rm E} a \tag{33}$$

From the limiting current (Equations 19 and 20) the mean velocity, v_z , of the active species to the RDE can be derived

$$v_z = \frac{I_1}{nFAc^s} = 0.62D^{2/3}v^{-1/6}\Omega^{1/2}$$
 (34)

From Equations 33 and 34 it follows

$$v_{\rm p}/v_z = 0.645 \,\Omega D^{-2/3} v^{-1/3} r_{\rm E} a \tag{35}$$



Fig. 19. The critical rotation speed (Ω_c) as a function of the particle size (2*a*) for the reduction of $(\Delta) K_3 Fe(CN)_6$ and (+) ZnO.

For the critical value, $(v_p/v_z)_c \sim \Omega_c a$. If this critical value $(v_p/v_z)_c$ is constant: $\Omega_c \sim 1/a$. This was found experimentally. It follows that for small particles Ω_c will be very high, i.e. beyond practical application. This explains why Vydra [27] did not observe an influence of very small silica particles.

4.4. Adhesion

Another explanation for the origin of the critical rotation speed is given by Leitel *et al.* [28] and Caprani *et al.* [16–19]. The occurrence of one or more critical values of Ω is attributed to partial blockage of the electrode surface by adhesion of particles and removal of adsorbed species at higher rotation speeds.

Careful analysis of the log *I* versus log Ω plots of Caprani *et al.* [16–18] with Al₂O₃ suspensions shows that even three transitions in Ω are found for small particle size ($2a \leq 3 \mu m$). At rotation rates below the lowest transition, Ω_0 , the current of the RDE is less than the current without particles. This indicates blockage of the electrode. However, for the SiC particle size > 3 μm , no reduction of the limiting current is observed. As explained before, the larger particles does not reach the electrode, therefore the two transitions, Ω_1 and Ω_2 , cannot be due to a blockage of the electrode. However, the value Ω_0 , which only appears for very small particles of Al₂O₃ suspensions ($2a \leq 3 \mu m$), is related with a transition to an electrode blocked by particles.

In a log-log plot of the I_1 versus Ω relation (see Fig. 20) of our results for SiC particles of $6.6 \,\mu m$, also show only two transitions in the rotation frequencies, Ω_1 and Ω_2 , as well as three different slopes, p_1 , p_2 and p_3 . The critical frequency, Ω_c , in the Levich plot is somewhat greater than Ω_1 . The slopes p_1 and p_3 are nearly 0.5, according to the Levich relation. The value of p_2 varies with the volume fraction of the particles and changes from 0.5 for low fractions to 0.65 for volume fractions of 40%. Therefore, some misfits exist in the Levich plots in the region of Ω_c . The influence of the particles becomes noticeable just above Ω_1 and increases to the rotation speed Ω_2 . Above Ω_2 , no further increase due to the particles is seen, only an increase with a slope of 0.5 according to the Levich equation. The force of adhesion between a particle and the electrode is given by Visser [29].

$$F_{\rm a} = \frac{A_{132}a}{6h^2}$$
(36)

 A_{132} is the Hamaker constant between the particle (1), electrode material (2) and the electrolyte (3); *h* is the distance between particle and electrode.

The force acting on a particle by the flow to the RDE is a corrected Stokes force [29] and is

$$F_{\rm s} = 10.2 \,\pi \eta a v_{\rm c} \tag{37}$$

with $v_{\rm c} = a\dot{\gamma}$.

The force acting on a particle by centrifugal acceleration can be neglected at the electrode surface. Introducing the shear rate at an RDE (Equation 32),



the force $F_{\rm S}$ is

$$F_{\rm S} = 25.6 \,\Omega^{3/2} v^{-1/2} r_{\rm E} a^2 \eta \tag{38}$$

At the critical frequency for the particle leaving the electrode $F_{\rm s} = F_{\rm a}$, thus

$$\frac{A_{132}}{6h^2} = 25.6 \,\Omega^{3/2} v^{-1/2} r_{\rm E} a \eta \tag{39}$$

This gives for the critical Ω value: $\Omega_c \sim 1/a^{2/3}$. This does not completely agree with the experimentally-found relation $\Omega_c \sim 1/a$ (see Fig. 19). Together with the fact that no limiting currents are measured that are lower than the Levich value (as explained before), adhesion is not a possible cause.

5. Conclusions

The mass transfer due to the reduction of 0.05 M K_3 Fe(CN)₆ in 2 M KOH at the RDE is increased by the presence of suspended SiC particles. The extent of the increase depends on the volume fraction. The experimental results, expressed as I_1 versus $\Omega^{1/2}$ relations, shows a critical value for both the volume fraction of SiC particles, ϕ , and the rotation speed, Ω , beyond which the presence of the particles becomes effective for mass transfer. A model is developed based on a diminishing of the diffusion layer thickness due to rotation of the particles in this layer. This yields a modified Levich equation, which takes into account the volume fractions of the particles, ϕ

$$I_1 = B\Omega^{1/2} \left[1 + \left(\frac{r_0}{a} \right)^3 \phi \right]$$
(23)

It is argued that the occurrence of Ω_c and ϕ_c is not due to a change in hydrodynamic conditions nor a blockage of the electrode. From experiments with an



upside-down cell, it is concluded that the appearance of ϕ_c is caused by gravitational forces. The results with this cell give good agreement with the model for all volume fractions if $\Omega > \Omega_c$.

The particle size does not play an important role except for particles larger than δ_N , where some deviation is found. The minimal approach, z_0 , between particle and electrode surface can be calculated. If $z_0 \ge \delta_N$, the particles cannot affect the mass transfer to the electrode. It is further concluded that the peripheral velocity of the rotating particles must exceed a critical value in order to contribute to enhanced mass transfer. It can be shown that a critical rotation rate Ω_c must exist that is proportional to 1/a. This was confirmed experimentally.

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